

Lines: Lesson 10

Direct Variation: Worksheet 1

answers

MATH ALL

Name: _____

Direct Variation lines always go through (0 , 0).

They are written in the form: $y = \underline{k} \cdot \underline{x}$.

Write the direct variation equations:

- The amount of gasoline we use directly varies with how many miles we drive:

$$\underline{g = k \cdot m}$$

- The height of a tree is directly proportional to how much water it gets:

$$\underline{h = k \cdot w}$$

Are these data sets examples of direct variation?

<table style="border-collapse: collapse; width: 100%;"> <tr> <td style="padding: 5px;">x</td> <td style="padding: 5px;">y</td> <td style="padding: 5px;">$k = \frac{y}{x}$</td> </tr> <tr> <td style="padding: 5px;">-3</td> <td style="padding: 5px;">-9</td> <td style="padding: 5px;">$-\frac{9}{-3} = 3$</td> </tr> <tr> <td style="padding: 5px;">1</td> <td style="padding: 5px;">3</td> <td style="padding: 5px;">$\frac{3}{1} = 3$</td> </tr> <tr> <td style="padding: 5px;">4</td> <td style="padding: 5px;">12</td> <td style="padding: 5px;">$\frac{12}{4} = 3$</td> </tr> </table> <p style="color: purple; text-align: center;">yes!</p>	x	y	$k = \frac{y}{x}$	-3	-9	$-\frac{9}{-3} = 3$	1	3	$\frac{3}{1} = 3$	4	12	$\frac{12}{4} = 3$	<table style="border-collapse: collapse; width: 100%;"> <tr> <td style="padding: 5px;">x</td> <td style="padding: 5px;">y</td> <td style="padding: 5px;">$k = \frac{y}{x}$</td> </tr> <tr> <td style="padding: 5px;">8</td> <td style="padding: 5px;">1</td> <td style="padding: 5px;">$\frac{1}{8}$</td> </tr> <tr> <td style="padding: 5px;">12</td> <td style="padding: 5px;">2</td> <td style="padding: 5px;">$\frac{2}{12} = \frac{1}{6}$</td> </tr> <tr> <td style="padding: 5px;">16</td> <td style="padding: 5px;">4</td> <td style="padding: 5px;">$\frac{4}{16} = \frac{1}{4}$</td> </tr> </table> <p style="color: purple; text-align: center;">no!</p>	x	y	$k = \frac{y}{x}$	8	1	$\frac{1}{8}$	12	2	$\frac{2}{12} = \frac{1}{6}$	16	4	$\frac{4}{16} = \frac{1}{4}$	<p style="color: purple; font-size: 1.2em;">$\frac{1}{8} \neq \frac{1}{6} \neq \frac{1}{4}$</p>
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y varies directly with x, and when x = 5, y = 2. What is y when x is 7?

$$y = kx \quad 2 = k \cdot 5 \quad y = \frac{2}{5}x$$

$$k = \frac{2}{5} \quad y = \frac{2}{5} \cdot 7 = \frac{14}{5}$$

y varies directly with x, and when x = 9, y = 3. What is y when x is 6?

$$y = kx \quad 3 = k \cdot 9 \quad y = \frac{1}{3}x$$

$$k = \frac{3}{9} = \frac{1}{3} \quad y = \frac{1}{3} \cdot 6 = \frac{6}{3} = 2$$

The amount of sprinkles varies directly with how many cookies are decorated. When 15 cookies are decorated, 2 grams of sprinkles are used. How many grams of sprinkles are used for 100 cookies?

$$S = k \cdot c \quad S = \frac{2}{15} \cdot c$$

$$2 = k \cdot 15 \quad S = \frac{2}{15} \cdot \frac{100}{1} = \frac{40}{3} \text{ grams}$$

$$k = \frac{2}{15}$$